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# Chladni meets Napoleon\*

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Abstract. Chileful belonged to those for scientist who have been able to assume combination for their work set only in predictional circles, but also in the lay public. During several journeys all over Europe Chileful demonstrated the sound afterne has discovered as well as the smooth interaction typication. In this respect the invitation prosonanced by Napoleon during a longer step in the parts to show the experiments at the insperiod cover use subsolubority a highlight. Chileful has given a personal report on this creat, in this serial is shall be trufted.

# 1 Introduction

On a February coming of the year 1890 in Paris, a curring showu up before Tailoric Paloce, the official residence of Nupsion Bioasparts, respect of the Franch people. The possessive wave the Count de la Place, chancelle of the senate, La Clopde, great chancelle of the Legion of Brancy, Bertheles, consist of the engine, and a Dr. Challed from Wittelener, Challed Paris which on a lecture tour through Durage. There he get to know the leading contemporary scientistic is proven, darpt from the three shortly mentioned, the mathematical Count of the Place, better known as Luplace, the channis Berthickt, and the biological La Cjobich, these were manning others Phonon, Sourt, and Blace, and an Assemble von Handshill, who storped in

Napoleon was interested in a demonstration of Chladmi's experiments and invited him to the Tulleries through the mediation of Laplace. While performing artists were rather often invited to court, the invitation of a scientist was a singularity. Chladmi has given a detailed personal account of his meeting with Napoleon, which will be represented later on.

But it is infer consider the year 1756, when Exact Freene Friedrich Chichis was been on Nov. 30th (see Fig. 14 for He].) It as a comparence of the Reformation in the 16th century. Wittenberg had become the critical centre of Europe due to the work of Lubberr and Schlendtchan, and the University Lowers of Wittenberg was considered the non-important the Chichies of Europe and the state of a proteined been in External Scane, and the university as well had bet it great renovae. Chichialir generalization, a proteined, had to be seen has not country Homoground uring the Counter-Deformation and settled with his family in Wittenberg in 1672. Chichialir generalization are proteined to the second with the Scane and the wittenberg and his factor was a professor of the height of Wittenberg, and his latter was a professor of the height of Wittenberg, and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was a professor of the height of Wittenberg and his latter was professor of the height of Wittenberg and his latter was professor of the latter was professor of the height of the was professor of the height of the latter was professor of the height of the latter was professor of the height of the height of the latter was professor of the height o

Chladni spent a sheltered youth. A bit too sheltered, as it seemed. Let us listen to Chladni's own words: "In my paternal house I was indeed kindly treated, and was well instructed by

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<sup>\*</sup> An abbreviated version of this article appeared in German in the November issue of the Physik-Journal Translation into English by E.-R. Stöckmann.

loasest and able teachers, but I had to submit to such restrictions that I could leaver the lower only on rare consisten, and never about, I could get to know enterly roung people of my age only in clurch. And, due to energetated care for the only san, I was merely allowed to get or Sixtee the special system to be granted one of the time spect companiedly induced as get Sixtee the age of six years the beg made use of the time spect companiedly induced as grant looked of goography and travels. At the age of features Chaladia was sent to the boursing-evident of crimma, and there as well the complained of a strongly restricted fereduct and movement

At the age of eighteen he took up low in Wittenberg. He would have much more preferred medicine, but yielded to the pressure of his father. At least he attained the permission to continue his studies in Leipzig. Here he fluidsdw with even two dissertations on philosophy and sine in 1732 and in 1732. Soon after his father disc. After years of turtleage be could now finally pursue his own interest. Instead of taking up have, which would have ansured him a occurred partner has been attained to the contract of the contract o

# 2 Discovery of the sound figures

Vitestians of lare and jutes some became his main field of interest, and in this domain he much the discovery which is associated with his same till today liet to intere to his personal much the discovery which is associated with his same till today liet also or much jutes of a size not too the contract of the contra

Actually Chladni was not the first to observe those vibration patterns. Leonardo da Vinci had already mentioned them in his note-book, and Galliei treated them in a longer passage of his Dialogo sopra i due massimi sistemi. It is, however, indisputable that Chladni was the first to examine the obseromence systematically.

After having renounced a legal profession Chladni had become a private scholar without a regular income. The money he got for guest lectures given at the University of Wittenberg was not sufficient to secure his living. Several applications for a prefessorial chair failed. This gave him the idea to earn his money by means of lecture tours: "It occurred to me that an artist

<sup>4</sup> Im witterlichen Hause ward ich reuze freumlich behandelt, und genodt von bezeen und geschlichten. Leberen geden Utzerricht, ward aber inmeer mit einer sochlen Einschräusigung gehalten, daß ich sur selten, und nie allein, ans dem Hause gehen deurfte, und andere junge Menschen meisen Alters nie andere, an der was in der Kirchen en sehen behange es ward mit sogar, am ützerrichenen Sengfalf heit abs dem einzigen Sohn, mer bei sehe gater Witterung verstattet, in dem am Hause befindlichen Hofeun Gaterin in die fert Left zu nechen.

Discoveries Concerning the Theory of Sound.
 Dialogue Concerning the Two Chief World Systems.

who knows how to give himself some publish give it is as attacked to those how to give himself some publish give it is as attacked to the opportunities of being received kindly and profiting nearly every see text an a-related desiration to a candemic life, and I lapsed to succeed like two the means of virtuosity, because I had so as let in life beyon to learn marked, but there is no late in life beyon to learn marked the virtual of a new internment. I thought myself more able to achieve it that many other man, because I had studied the nature of many a sounding body by theoretical.<sup>15</sup>

At first Chlodic had apposently not the slightest blee that the more demonstration of the sound patterns ontal by or interest for the general public. After a longer priced of trying and several wain experiments in 170 Chlodic finished his first invented instrument to which he gave the anhibtion name Euphon (Genet: exposure), i.e. beautiful sound.). The sound was produced by glass rods bringing about vibrations when excited by fifteines rods fixed perpendicularly to the size. He will, we have the contraction of the size for the first first better too rete ask. He will, profess of up the Euphon and his plates, Challed never the first first between too

It soon became evident that the public was actually interested in the sound patterns and not the new instrument. Fig. 2 of Ref. [1] shows Chiladi during a demonstration. It took place in the public of pricer Thurn and Taxis in Regensburg in 1800. In general the public was less interested in physics but simply in a good show. The sketch shows how Chiladin could bring about individual vibration patterns by fixing the plate at different positions between thumb

and index. Be developed an ingressive skill in excending this technique. In 1800 Chabil niversted a second musical instruments which be called Carleyfulder. The sound was produced by metallic vibration bars, similarly as had been the case with the Emploon. The excitation, bowever, was brought about via a notating cycliner against which the bar could be pressed by means of a key. The keys were arranged as those of the pians. Chibrid instruments appeared, manely the Medocken and the Terpolon which initiated by principle of

In 1802 Chladni moved from the house where he had been born to a flat in Schlossstr. 10.
In the same house Wilselm Weber grew up who became famous later on for his experiments on magnetism. At the age of only 21 he published a monegraph on the science of waves, together with his elder brother Ernst Heinrich, his senior by nine years. The book was dedicated to "our dear friend Chladni, the initiation of accounties based on exceptionaris."

dear friend Chidnii, the initiator of acoustics based on experiments."

In 1802 Chidnii's main work Die Akustä? appeared, in which he summarises every fact known in this field up to that period [3]. The main discoveries were Chidnii's own. Apart from the sound figures Chidnii was the first to observe longitudinal vibrations of bars. It is no exageration to state that acoustics has become a discipline of its own due to this book.

Since the theory on the vibrations of clustic plates did not yet culst, the description of the sound figures had to remain qualitative. Challed industible the pattern observed for rectangular planes according to the number of model into parallel to both sides, and be surgue to the starterally to the figure with the leasest frequency. Fig. 1 above, a plate from its Asichard artiturally to the figure with the leasest frequency. Fig. 1 above, a plate from its Asichard according to the starter of the starteral planes are supported by the starterally that the according to the starteral planes are supported by the starteral planes are in the starteral planes and the starteral planes are supported by the starteral

$$\nu \sim (n + 2m)^2$$
, (1)

today known as Chladni's law (see Ref. [3], p. 131).

<sup>5</sup> "det hatte dabei den Gefanden, daß ein Küntler, der einigt Aufmerkundeit in erregen weit, wenigen an einen bestimmten Om typenmeln ist und mehrere Gelegandeit hat, fast überall Vordrech ist, weit der eine gate Aufmahme en finden, als ein Geleberte, der ein dem Andemischen Leben wichnet, und hoffen des ankedmischen Leben wichnet, und hoffen des ankedmischen Leben wichnet, der eine gate Aufmahme en finden, als ein Geleberte, der ein dem Andemischen Leben wichnet, und ein weit gelegen, zuwar nicht der durch Virtussenstlerte, weit ich so gilt amgedange hatte Lein zu erferens, aber dech durch Erfindung eines neuen Instrumentes, welches ich eber, als ein Anderer zu erferens, aber dech durch Erfindung eines neuen Instrumentes, welches ich eber, als ein Anderer zu erferens, aber dech durch se ein den Vertrecht und der eine Stephen der der eine Stephen der der eine Vertrechte der eine Vertrechte

<sup>6 &</sup>quot;verehrtem Freunde Chladni, dem Begründer einer auf Versuchen beruhenden Akustik".

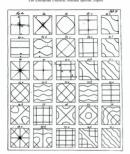


Fig. 1. Sound figures of a quadratic plate (E.F.F. Chladni, Die Akustik 1802 [3]).

On the consists of a visit to Weimar in 1930 Challeni not Goethe to whom he gave a copy of in book, in this consistent Goethe werker the fellowing in a letter to Sellinit: "Doct both the book in the consistence of the consistence of the consistence of the consistence of the of it and shall give you as somewhat agreeded cond report on its consistence, matches, and form. He belong to ... these blinding because who have not the failured that there is something as natural philosophy and who are only attentively trying to observe phenomena to the consistence of the consistency of the consistency of the consistency and the the matter and it returned for the matter? Office as well as the failure of the consistency of the matter and it returned for the matter?

As to the background of this not so flattering characterisation of Chladmi's personality, we can only speculate. Trying: "to observe phenomena and classify them well" is a characterisation of the experimental physicist, and can hardly be rated as a reproach movadays. As is generally known, Goethe regarded himself as a natural scientist and did not underrate his achievements in this field. May be Goethe had tried to convince Chladmi of his Town of Colours and had

<sup>\*</sup>Theter Chiada ist angelommen und hat veice assignetiester Atsatik in einem Querthand mittgebracht, ich habet eine dem ut Hälfte geleens und werde Basen derüber mindlich, über Inhalt, mittgebracht, ich habet eine dem und der Basen de

not provoked the enthusiasm he had hoped for. However, a few years later Goethe has made several positive statements on Chladni's behalf in public [1].

Another port, Toomas Mans, who liked to compuse himself to Gorthe, creets a literary monument to Chaldes. In the introductive chapter of his grat late novel Dr. Faustes the post introduces the inher of his hero Melina Levelilla. This inher lites to "speciality the contractive of the contractive contractiv

#### 3 Chladni in Paris

und ...

In 1907 Chilothis set off again on a long journey boding him via the Netherhands and Brossob to Paris, where he stayed from 1908 to 1810. This was the very period whem the absencemioned meeting with Napoleon took place. Let us again litten to Chilothi's corn scotic: When I entered, the sedement of the corn, with the expression of his force. Except him there were also present his sponse Josephine, a will bountful and charming lady, his mother him there were also present his sponse Josephine, a will bountful and charming lady, his mother of the control of t

"I first played some pieces on the Clarkeylinder which seemed to please the persons present. Napoleon did also want to produce some somath, but though I had tdad him that the keys must only be pressed very softly, and although he did believe to have pressed them very softly, it happened so vigorously that in my opinion even this showed that his energy dominated his softness." <sup>10</sup>

Subsequently Chladni demonstrated the sound figures: "Napoleon showed much interest in my experiments and explanations, and asked me, as an expert in mathematical questions, to explain all topics thereughly, so that I could not take the matter too easy. He was well informed that one is not yet able to apply a calculation to areas curved in more than one direction, and that, if one were successful in this respect, it could be useful for applications to other subjects

Napsdom and science could be the topic of a whole easy of its own. He actually had an excellent knowledge of mathematics, as we get to know from his chool reports. And when in 1796, he was still a young general at this period, his trespues plumbered Pevis, he gave orders to sparce the homes of the university professors, among them the home of Absandre Volta (L. Leter on in Paris, in 1801, Volta also got the chance to present his experiments to Napsdom Bonquarte, who was then still the first consul of the French republic, As we have already

leurnt, the leading scientists held high positions at the imperial court. Later on Laplace was even appointed marquis.

<sup>9</sup> "Als ich citarta, empfing er mich, in der Mitte des Zimmers stehend, mit Aeusserungen des Wohlwollem. Auser ihm waren nech rugegen seins Gemahlin Josephine, eine damals nech sehr wohlgebäldete, liebenwirdige Dome, seine Mutter Littis, deren Annehe und Beachmen Gestatiskigheit von

<sup>193</sup> "Ich spielte erst etwas auf dem Clavicylinder, welches den Anwesenden zu gefallen schien; Napoléon wollte hierauf auch einige Töne angeben, aber, wiewold ich ihm gesagt hatte, dass die Tasten nur sehr gelind missten niedergeptrückt werden, und er sie auch nur sehr schwech niederzudrücht en glaubte, so geschah es doch mit solcher Stärke, dass meines Erachtens auch hierin seine mehrere Energie als Saufheit ich zu erkeinen gah?

<sup>11</sup> "Nagolów benégie melnen Experimenten und Edificangen vide Anfanchamheit, und verlanger, als former annahmentierte Gagenstände, dass ich in all. Mare reitst von Gerud om erfellten sollte, so dass ich als ode Sache und Gene dass erfellten sollte, so dass ich als ode Sache nickt eben von der heideten Selte zehnen darfte. Er wusste auch reicht woll, dass man mehn inder in Stande ist, Fleisben, die nach mehn des einer Reitung auf verseheidenen Art gelvirannet sind, so dem Calvail en unterwerfen, wie brunnet Lüiser, dass, wesen man Berin swirere gelvirannet sind, so dem Calvail en unterwerfen, wie brunnet Lüiser, dass, wesen man Berin swirere wirder."



Fig. 2. Dedication of the Truité d'Acoustique to Napoleon.

The next marring Chicking at a gravity of 6000 frame, connected to the request to publish the Adustat in French to design this work Chicking consumers of publish. For the Grammar terms Schold, Zhong, and Too, used by Chicking with direct meanings, the French language and publish more encourage, nounders are, i.e. South A. Frenchman is easily absorb this matter gave him the following asserve; which was not very heighth "Swher disablesse the images are sent up no grider a Trapersonic in their to its side as possible. If pull rating englishes marrifer use the climinated the out-of-sidest and adule me ideas. In November 1900 the book was published under the title of Tarit's Allowandrye, Chickins made the following remark: The regulation grife rouse the from the bookships were those the French scientists usually reviewed by physical or mathematical form the bookships were those the French scientists usually reviewed for physical or mathematical to the contract of the state of the name of the state of the name of the state of the name of the state of the name of the state of the name of the state of the name of the state of the name of the state of the name of the state of th

Galactic department the book to the Northean and the Conference of the Conference of

<sup>12 &</sup>quot;Our desil of a language does not want to lend itself to the expession of all ideas possible. Sometimes it is even necessary to sucrifice an idea to the caprices of the language."

at is even nozssary to sacrifice an stat to the caprocs of the tanguage.

13 "Das von der Burkhandlung entricktete Honorer war überigens eben so, wie es gewölmlich die dortigen wissenschaftlichen Männer für physikalische oder mathematische Bücher erhalten, welches aber doch bei weitem nicht so Viel beträgt, wie etwa das Honorar für Schriften von Frau von Staël und Anderen, die ein weit grüsseres Publikum haben.

Annoren, nor em west gesseres russecum nacen.

"It" "Die meiste Mühe hat mir die nicht zu vermeidende Dedication gemacht. Es wollte mir nümlich nicht gelingen eine épitre dédicatoire absudassen, mit der man recht wäre zufrieden gewesen, und in der man auf der einen Seite alle Schmeichelei (die meine Sache nicht ist) vermieden, und auf der anderen Seite doch alle gebührende Achtung und Dankbartsteit ausgedrückt hätte. Endlich noch ich mich aus der

cet ourrage, après en avoir su les expériences fondamentales.<sup>21</sup> Perhaps that was what really happened. There is, however, good reason to be doubtid. In 1826, when Chladni drew up his report, conditions in Europe had dramatically changed. Some years before Napoleon had died on St. Helena, and an atmosphere of repression reigned all over Europe. The dedication had thus become a problem.

In solition to the personal grainty for Chabdan Napoleon held out a price of 2000 frames for the mathematical theory of the sound patterns. In 1816 the price was senseded Sophie Germain for an easy entitled Rederenkes are in theire: doe analyses chaniques. "Home the contract of the hall been desired to be risk had therefore accepted the accessing between glories discussing site of the contraction. She made some important contributions to number theory, and exchanged scientific letters with comes, in the beginning under an assumed mits man, sade foreir a weansa would not be

Sophie Germain's explanation of the sound patterns was incomplete. The prize was given to her all the same since it was acknowledged that her treaties signified an escential progress. The problem proved to be obtained. The complete solution for deviate plates was found by the property of the contract of the contract plates was found by the property of the property

Calcula figure of tergology shaped plate. here experienced a superior appealing repolarly monology. The room is the equivalence between the attainancy was equation, the Heimbell exquation, and the attainancy Schrödinger equation for a particle moving ferrly in a low with reflecting with. The module the examination of such quasars builded, and, in the new reduction of the state o

useful when applied to other objects, "on only be colled visionary,"
After a long absence Childed internated to commany the Striterization and Raly in the summer
of 1812. He consisted flower and Nogles, "since the reads beging there were too must because
the control flower and Nogles, "since the reads beging the very two the second because
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two more to the small count of Kenderg, situated in Stikematters to the south of the host reads in
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the same on the same year the find to be the same of the liberalges, many the fine Beginning
and the Carloty-timer. As we know from a report of the young Falti Mondelsoush-Barthelly,
which had visible Children's formed as in Karderian [181], the led beats heart control or control or site of the terminant of continuous plants and the Carloty-timer. As we know from a report of the young Falti Mondelsoush-Barthelly,
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when the property of the young Falti Mondelsoush-Barthelly,
when the property

In Kemberg Chladni spent the rest of his life, only interrupted by the still numerous lecture tours. During one of these he died in Breslau on April 4th 1827.

Verlegenheit auf eine Art, mit der man allgemein zufrieden war, nämlich durch folgende Dedication im Lapidarstyl:

15 Napoléon the Great has deignod to accept the dedication of this work, after he had seen the pertinent

— Napotom the Great has despined to accept the dedication of this work, after he he fundamental experiments.
10 Research on the Theory of the Elastic Surfaces.

17 "Was die strenge mathematische Theories betrifft, so ist sie wohl erst nur in wenigen Fällen dahingelangt, Resultate zu liefern, die albeitig eine Anwendung auf das Esperiment gestatten."
13 "weil die Wege derthin wegen der vieles Straßensiaber und Mörder gar zu unsicher waren."

### 4 Résumé

With good remon Chichia is regarded as the father of counties. Here we must not leget that he had also done pioners work in a bridge different field by the last field restart in the last had been proposed to the control of the last had been proposed by the pomerys Chichial scient every apportunity to comple any knowledge of neterorities which could be nount in theirses. It is emanatical the families in the fillering expery published in 17th, the foundation of the control of the con

As Chichait tells us, be was offers pitted for his unsteady life: "Some have been so kind as todpione no sometant anomale way of living, since I have settly meet received a call, and todpione and the contract anomale way of living, since I have settly meet received a call, and been a disadvantage for science are for myreld. If I had get a position in a particular pitch second for distinguish writer such as extensive illensy can be consulted, I would have meller been able to work properly on accounts now on the teaching of the method remarks and the contract and

Childra was born in the same year as Monart, and doed in the same year as Borthorn. We have listed of a man has been? The general modifies of players (Suppless Boosparty)? The solution of gains (Lebrander v. Harsdolf)? Morel's a modified processing (Adam Wellgang associated to provide incess. There is, however, made to be said for it full Childra's preconsiderate the protein fears. There is, however, much to be said for it full Childra's preconsiderate the provide fears of the contribution of the provide provide and the contribution of the contribution of the contribution of the contribution of the contribution is necessarily as a contribution of the contribution of the contribution of a more laberted in the contribution is contributed in the contribution to south and the contribution is contributed in contribution to account and to the desire of meteories, which these permanent effects in the contribution to account and to the desire of meteories, which were a present effects of the contribution to account and to the desire of meteories, which were a present effects of the contribution to account and to the desire of meteories, which were a present effects of the contribution to account and to the desire of meteories, which were a present effects and the contribution to account and to the desire of meteories, which were a present effects and the contribution to account and to the desire of meteories, which were a present effect of the contribution to account and the desire of meteories, which were a contribution to the contribution to account and the desire of meteories, which were a contribution to account and the desire of meteories, which were a contribution to account and the desire of meteories, which were a contribution to account and the desire of meteories, which were a contribution to account and the desire of the contribution to desire of the contribution to account and the contribution to account and the contribution to account a contribution to account and the contribution to account a desire of th

In writing this paper I could widely go back to Chladmi's original quotations. In the introduction to the Akustik [3] as well as in the Neue Beiträge zur Akustik [12] Chladmi gave adetailed survey of his life,

<sup>&</sup>lt;sup>19</sup> On the Origin of the Iron Masses Found by Pallas and Others Similar to it.

<sup>&</sup>lt;sup>20</sup> "Obgleich seit dritthalbtausend Jahren die Annalen der Völker von Steinfällen erzählen, mehrere Beispiele derselben durch unverwerfliche Augsneuegen ausser allem Zweidel gesetzt waren........... so ist den bis auf Chalsdra, der schon durch die Endelschung einer Klungiguren sich ein unsterblichen Verfüsst um die Physik erworben hatte, ein so grosses Phäsomen fast unbeobachtet, in seinem innigen Zusammenhange mit dem übrigen Plaustenerstenen unerhangen gehölen."

<sup>&</sup>lt;sup>28</sup> "Motiver sind or gettability growers, mith wegen meiner etwas nomicident Lebeusevies are behauters, wit ich dem ands withfirth in eiden Bull, an weigsjerts einem annömlichen Hof zur begroot fram belle einhalt hier. Ich find also hat die dem weiter die behaufe für die Wissenstahl, war was der der die behaufe für die Wissenstahl, wo mas eine so weiterhaltige Bibliethe benehmte konn, ausgehört werden, zu wirde die weder die Abstath, noch die Lebeu von dem Abstermannen haben gehörig bestehelts werden, zu wirde den selbere freihnige selfenfelte hat, zu jahl dellet und dass felbere Dischaltungsun und Usternehmagen Anderer

which is very unusual from the actual point of view. Chladni's report on his meeting with Napoleon is reprinted in the essay on Chladni's life and work by F. Melde [11].

I am indebted to my wife E.-B. Stöckmann for the translation of this article.

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